



stage coupler to increase the operating bandwidth in terms of return loss thereby increasing VSWR at the operating frequency of 2.4GHz. The branch line hybrid also has the advantage that it may be realized using slot lines in the ground plane of a microstrip circuit. In this case the hybrid requires virtually no additional real estate on the chip-[2].

## II. DESIGN & CALCULATIONS

The geometry of a two stage coupler is shown below.

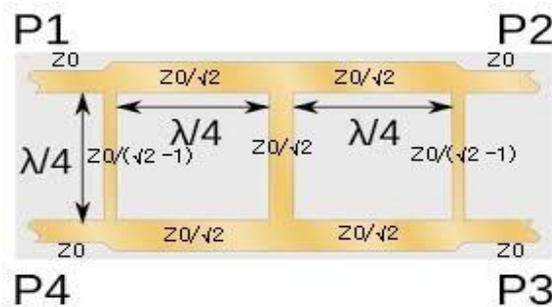


Fig 1: Geometry of a two stage Branch-line Coupler

The figure shows different values of impedances at the various arms of the coupler. In accordance to the impedances the length and width of the various arms changes. As we see, from the figure 1, the three different values of impedances are present on different arms of the coupler, thus, we have 3 different lengths and widths for these three values of impedances. As we are using a characteristic impedance( $Z_0$ ) of 50 ohms, The other two values of impedances namely ( $Z_0/\sqrt{2}$ ) and ( $Z_0/(\sqrt{2}-1)$ ) are calculated using this value of  $Z_0$ . We get their values as 35.3553 ohms and 120.7106 ohms. Thus we have to calculate the lengths and widths for each of these impedances. There are two methods of calculating the length and breadth: (1) using formulae and (2) using line calculator

Discussing the second method first, the line calculator is an inbuilt calculator in ADS used for the calculation of length and width for a particular impedance associated coupler arm. The parameters required for the calculation includes substrate height, cover height, conductor height and conductivity, permittivity, loss tangent, electrical length etc. Regarding the first method, we use the various formulae to calculate the length and width as follows;

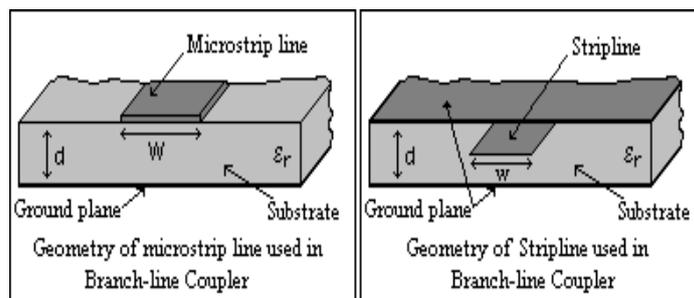


Fig 2: Geometry of microstrip line

The w/d ratio can be obtained as below;

$$\frac{w}{d} = \frac{8e^A}{e^{2A}-2} \quad \text{for } w/d < 2 \dots \dots \dots \text{eqn [1]}$$

$$\frac{w}{d} = \frac{2}{\pi} \left[ B - 1 - \ln(2B - 1) + \frac{\epsilon_r - 1}{2\epsilon_r} \left\{ \ln(B - 1) + 0.39 - \frac{0.61}{\epsilon_r} \right\} \right] \quad \text{for } w/d > 2 \dots \dots \dots \text{eqn [2]}$$

Where,  $A = \frac{Z_0}{60} \sqrt{\frac{\epsilon r + 1}{2}} + \frac{\epsilon r - 1}{\epsilon r + 1} \left( 0.23 + \frac{0.11}{\epsilon r} \right)$  .....eqn [3]

$B = \frac{377\pi}{2Z_0\sqrt{\epsilon r}}$  .....eqn [4]

Taking substrate height as 1.6mm,

1) for  $Z_0=50$  ohms

$\epsilon_r= 4.4$ ,  $f= 2.4$ GHz,

Assuming  $W/d \leq 2$ , we get  $A=1.5713$

$W_1/d=1.8193$

Which means our assumption was right,

$W_1=2.910$ mm

2) for  $Z_0=35.35$  ohms

Assuming  $W_2/d \geq 2$ , we get,

$B=7.7261$

$W_2/d=3.0571$

Which means our assumption was right

$W_2 = 4.8913$ mm

For the calculation of width the following formula can also be used;  $w = \frac{7.48h}{e^{Z_0\sqrt{\frac{\epsilon r + 1.41}{87}}}} - 1.25t$

.....eqn[5]

We may also note that the length for the impedances 120.7 ohms and 35.35 ohms are different by more than 1mm, but owing to the geometry of the coupler in figure 1, we conclude that if these two lengths are taken different, the layout of the coupler is disturbed affecting the result. Thus we take this length same for both the impedances and compensate this change in length by adjusting the width. Finally we obtain the length and width of the impedances as follows;

Impedance	Length	Width
50 ohms	17.13900 mm	2.986770 mm
35.3553 ohms	17.58097 mm	5.113680 mm
120.7106 ohms	17.58097 mm	0.3355921 mm

*Table 1: Length & Width for available coupler arms*

### III. SIMULATION

For the purpose of simulation the software used is Advanced Designing System (ADS). Beginning with the simulation the very first step involves developing the schematic by connecting the various impedances associated with the coupler arms and terminating each of the ports with matched terminations to perform the simulation.

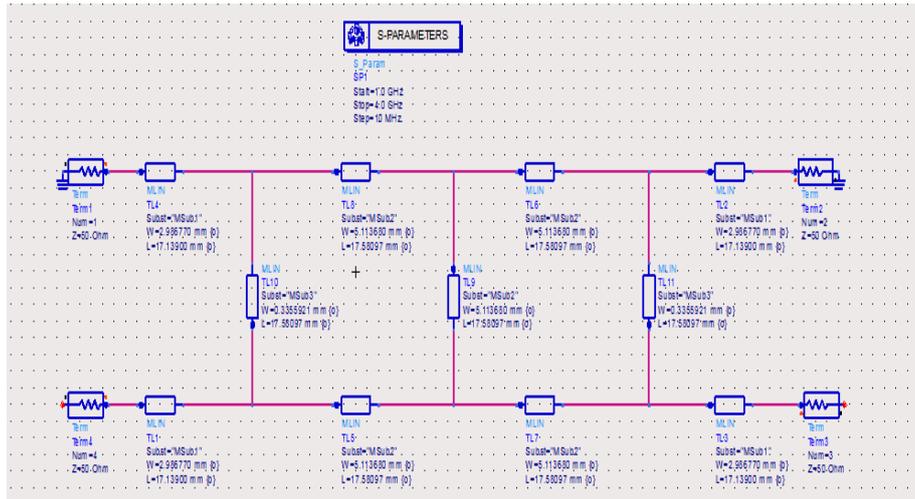


Fig 3: Schematic of the two section hybrid coupler

The various results are obtained for the magnitude of s parameters. Also the phase difference between  $S(3,1)$  and  $S(2,1)$  is obtained. The various results obtained after the simulation are shown below;

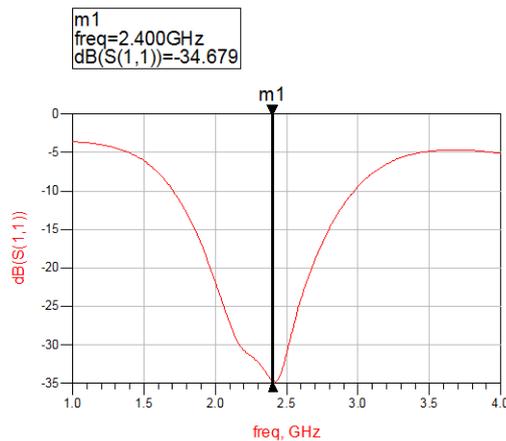


Fig 4(a): Magnitude of S11

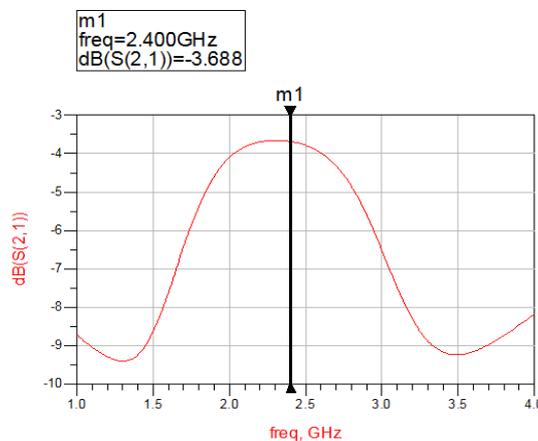
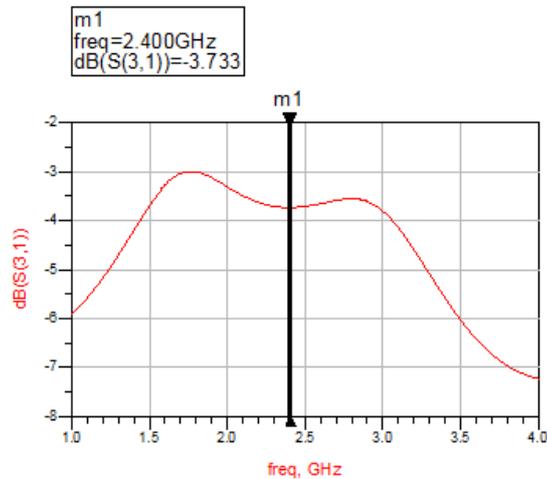
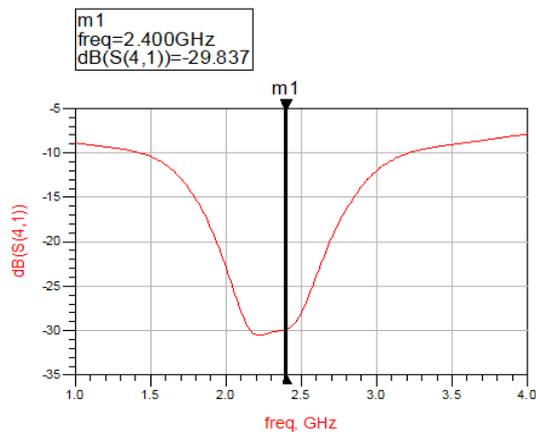


Fig 4(b): Magnitude of S21

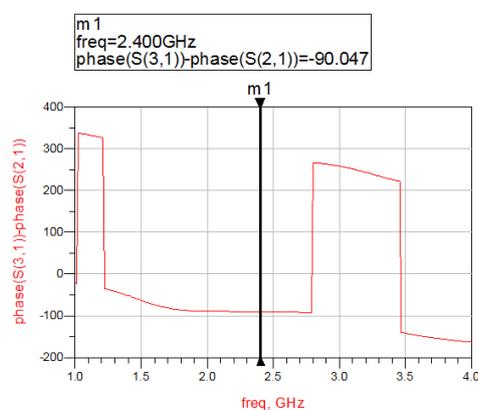


**Fig 4(c): Magnitude of S31**



**Fig 4(d): Magnitude of S41**

The simulation is performed and the various results obtained are presented in figure 4(a), figure 4(b), figure 4(c), figure 4(d). The various results are obtained for the frequency range of 1 GHz – 4 GHz, however, the coupler was designed to operate for a centre frequency of 2.4 GHz and hence the various results are checked for the frequency of 2.4 GHz. The software gives the freedom to plot the equations as per user requirements. We use this feature of the software to plot the phase difference between S31 and S21 shown in figure 5.



**Fig 5: Phase difference between S31 and S21**

The figure 6 shown below shows the layout of the coupler which is obtained using the same software. The layout is generated to perform the EM simulation which is a process depicting the real time performance of the coupler under non ideal conditions. The EM simulation was performed using substrate as FR4, substrate thickness as 1.6mm, conductor thickness as 0.035mm, permittivity as 4.4 and the center frequency as 2.4GHz. In real time, a cover is included for the purpose of protecting the substrate from external damage. Hence, in EM simulation the cover is also included and the cover height is also considered and it is taken as 12.8mm. The output of EM simulation is shown in figure 7.

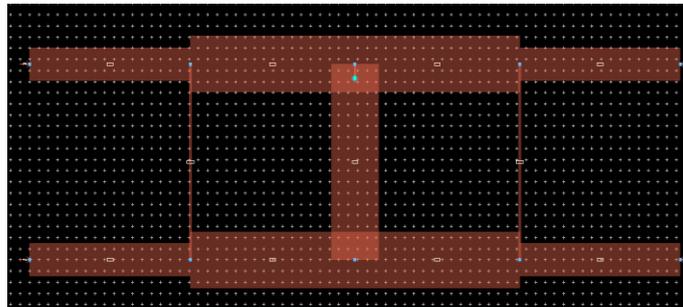


Fig 6: Layout of the Two Section Hybrid Coupler

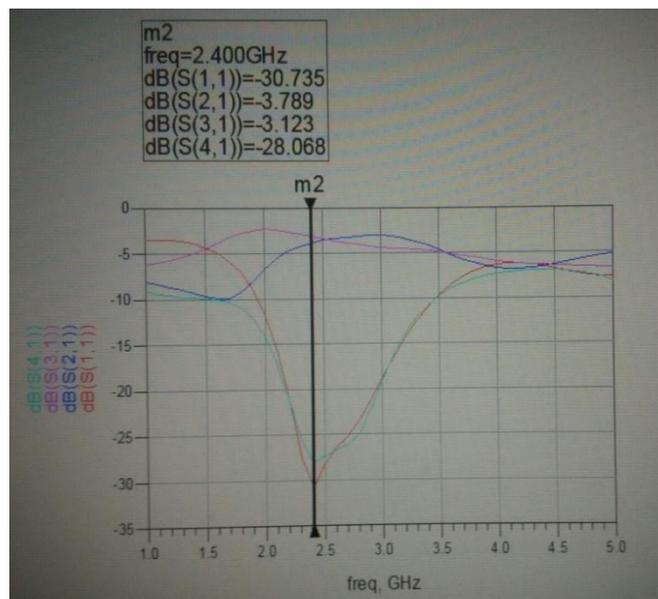


Fig 7: Results of EM Simulation

#### IV. RESULT AND DISCUSSION

As observed from previous section the various outputs are obtained for normal simulation using the schematic as well as the EM simulation using the layout. The tabular representation of the results are shown;

S parameters	Simulation	EM Simulation
S11	-34.679	-30.735
S21	-3.688	-3.789
S31	-3.733	-3.123
S41	-29.837	-28.068

Table 2: Results of normal and EM simulation

The values obtained for s-parameters in ideal conditions are quite in agreement with the values obtained in real time environment under non ideal conditions. The value of return loss obtained for a two stage coupler is better than the value for single stage coupler, as well as, the other s-parameters of a two stage coupler are also having decent values as compared to a single stage coupler. The operation frequency range is slightly greater than 1.2 GHz which is an increased range as compared to the single stage coupler which has a range of 1 GHz or less than that. Thus the bandwidth increases by more than 20%. Also the phase difference obtained between port 3 and port 2 is -90.047 which was the desirable value. VSWR can be calculated using the value of reflection coefficient which can be obtained using S11 as given below;

$$\Gamma = 10^{(S11/20)} \dots\dots\dots \text{eqn [6]}$$

$$\text{VSWR} = (1 + \Gamma) / (1 - \Gamma) \dots\dots\dots \text{eqn [7]}$$

The value of VSWR obtained from above equations is 1.03.

Finally, we present a comparative study between a single stage and two stage directional coupler regarding the performance;

Parameters	Single Stage Coupler	Two Stage Coupler
S11	-30.727	-34.679
S21	-3.661	-3.688
S31	-3.652	-3.733
S41	-35.393	-29.837
VSWR	1.05	1.03

### V. CONCLUSION

We have successfully implemented a two stage branch-line hybrid coupler using microstrip technology. The two stage coupler gives an improved value of VSWR as compared to the single stage coupler. The increase in operating bandwidth is another advantage. However, increasing the number of stages increases the area to be occupied. The proposed coupler exhibits low insertion loss, good return loss as well as acceptable quadrature phase shift between output ports. This prototype can be integrated into the design of microwave or millimeter-wave integrated circuits where the compactness of components is crucial.

### REFERENCES

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